

PHILOSOPHY TRIPOS Part II

Tuesday 30 May 2006

9 to 12

Paper 7

MATHEMATICAL LOGIC

Answer **three** questions only.

Write the number of the question at the beginning of each answer. If you are answering the either/or question, indicate the letter as well.

STATIONERY REQUIREMENTS

20 Page Answer Book x 1

Rough Work Pad

**You may not start to read the questions
printed on the subsequent pages of this
question paper until instructed that you
may do so by the Invigilator**

- 1 Compare and contrast first-order and second-order logic.
- 2 Is second-order discourse about all sets permissible?
- 3 ‘Axiomatizing set theory leads to a relativity of set-theoretic notions’ (Skolem). Discuss.
- 4 Show that categorical theories are complete. Outline which first-order theories are categorical, explaining how treating identity as a logical constant affects the situation.
- 5 Does the iterative conception of set resolve Russell’s paradox?
- 6 Develop an account of the arithmetic of transfinite ordinals. Discuss examples of arithmetical laws that generalise to the transfinite case, and examples of laws that do not.
- 7 Is the axiom of choice true?
- 8 Outline carefully one proof of Gödel’s First Incompleteness Theorem. Comment on the presuppositions of your proof.
- 9 **Either** (a) ‘We can hope that arithmetic is consistent, but we cannot hope to prove it is.’ Discuss.
Or (b) ‘Gödel’s Second Theorem conclusively shows that Hilbert’s Programme fails.’ Discuss.
- 10 ‘Church’s Thesis is in principle refutable but not provable.’ Discuss.

END OF PAPER