PHILOSOPHY TRIPOS Part IB

Friday 20 May 2016

09.00 - 12.00

Paper 2

LOGIC

Answer three questions only.

Write the number of the question at the beginning of each answer. If you are answering the either/or question, indicate the letter as well.

STATIONERY REQUIREMENTS

20 Page Answer Book x 1 Rough Work Pad

> You may not start to read the questions printed on the subsequent pages of this question paper until instructed that you

may do so by the Invigilator

- 2 -
- 1. What does the compositionality of meaning explain?
- 2. EITHER (a) What does the liar paradox show us about truth?

OR (b) 'The expression "...is true" is a meaningful predicate. So truth must be a property.' Discuss.

- 3. 'It is absurd, but to some people it is also easy, to be misled by the grammatical similarity of "Somebody came" to "Nobody came" into the misconception that "Nobody" refers to a person just as does "Somebody". Discuss.
- 4. Is an invalid argument invalid in virtue of its form?
- 5. Is Frege's notion of the sense of a singular term coherent?
- 6. 'Sin 90° = 1. Cos 90° = 0. Tan $x = \sin x/\cos x$. So tan 90° = 1/0.' Formalize this argument, discussing any problems that arise.
- 7. Answer both parts of this question.
 - (i) A relation *R* is weakly dense if $\forall x \forall y (xRy \rightarrow \exists z (xRz \land zRy))$. Show that the formula $\Box \Box p \rightarrow \Box p$ is a logical truth of the modal logic of weakly dense Kripke models, but $\Box p \rightarrow \Box \Box p$ is not.
 - (ii) Show that the formula $\Box p \rightarrow \Box \Box p$ is a logical truth of the modal logic of transitive Kripke models, but $\Box \Box p \rightarrow \Box p$ is not.
- 8. Are the meanings of the logical constants given by their inference rules?
- 9. 'If the arbitrarily given axioms do not contradict one another with all their consequences, then they are true and the things defined by the axioms exist.' (HILBERT) Discuss.
- 10. Answer both parts of this question.
 - (i) Outline a proof of the Disjunctive Normal Form Theorem via truth tables.
 - (ii) Outline a proof of the Conjunctive Normal Form Theorem via substitution.